

# Semantic Parsing with Combinatory Categorical Grammars

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## Language to Meaning



## Language to Meaning

Information Extraction

Recover information about pre-specified relations and entities



Example Task

Relation Extraction



*is\_a(OBAMA, PRESIDENT)*

## Language to Meaning

Broad-coverage Semantics

Focus on specific phenomena (e.g., verb-argument matching)



Example Task

Summarization



Obama wins election. Big party in Chicago. Romney a bit down, asks for some tea.

## Language to Meaning

Semantic Parsing

Recover complete meaning representation



Example Task

Database Query

What states border Texas?



Oklahoma  
New Mexico  
Arkansas  
Louisiana

## Language to Meaning

Semantic Parsing

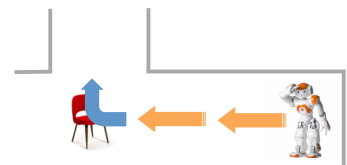
Recover complete meaning representation



Example Task

Instructing a Robot

at the chair,  
turn right



## Language to Meaning



Complete meaning is sufficient to complete the task

- Convert to database query to get the answer
- Allow a robot to do planning

## Language to Meaning



at the chair, move forward three steps past the sofa  
 $\lambda a.pre(a, ix.chair(x)) \wedge move(a) \wedge len(a, 3) \wedge dir(a, forward) \wedge past(a, iy.sofa(y))$

## Language to Meaning



at the chair, move forward three steps past the sofa  
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## Language to Meaning

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$f : \text{sentence} \rightarrow \text{logical form}$

## Language to Meaning

at the chair, move forward three steps past the sofa



$f : \text{sentence} \rightarrow \text{logical form}$

## Central Problems

Parsing

Learning

Modeling

## Parsing Choices

- Grammar formalism
- Inference procedure

Inductive Logic Programming [Zelle and Mooney 1996]

SCFG [Wong and Mooney 2006]

CCG + CKY [Zettlemoyer and Collins 2005]

Constrained Optimization + ILP [Clarke et al. 2010]

DCS + Projective dependency parsing [Liang et al. 2011]

## Learning

- What kind of supervision is available?
- Mostly using latent variable methods

Annotated parse trees [Miller et al. 1994]

Sentence-LF pairs [Zettlemoyer and Collins 2005]

Question-answer pairs [Clarke et al. 2010]

Instruction-demonstration pairs [Chen and Mooney 2011]

Conversation logs [Artzi and Zettlemoyer 2011]

Visual sensors [Matuszek et al. 2012a]

## Semantic Modeling

- What logical language to use?
- How to model meaning?

Variable free logic [Zelle and Mooney 1996; Wong and Mooney 2006]

High-order logic [Zettlemoyer and Collins 2005]

Relational algebra [Liang et al. 2011]

Graphical models [Tellex et al. 2011]

## Today

Parsing

Combinatory Categorical Grammars

Learning

Unified learning algorithm

Modeling

Best practices for semantics design

Parsing

Learning

Modeling

Parsing

Learning

Modeling

- Lambda calculus
- Parsing with Combinatory Categorical Grammars
- Linear CCGs
- Factored lexicons

Parsing

Learning

Modeling

- Structured perceptron
- A unified learning algorithm
- Supervised learning
- Weak supervision

Parsing

Learning

Modeling

- Semantic modeling for:
  - Querying databases
  - Referring to physical objects
  - Executing instructions

## UW SPF

Open source semantic parsing framework

<http://yoavartzi.com/spf>

Semantic  
Parser

Flexible High-Order  
Logic Representation

Learning  
Algorithms

Includes ready-to-run examples

[Artzi and Zettlemoyer 2013a]

Parsing

Learning

Modeling

- Lambda calculus
- Parsing with Combinatory Categorical Grammars
- Linear CCGs
- Factored lexicons

## Lambda Calculus

- Formal system to express computation
- Allows high-order functions

$$\lambda a. \text{move}(a) \wedge \text{dir}(a, \text{LEFT}) \wedge \text{to}(a, \text{vy.chair}(y)) \wedge$$

$$\text{pass}(a, \text{Ay.sofa}(y) \wedge \text{intersect}(\mathcal{A}z.\text{intersection}(z), y))$$

[Church 1932]

## Lambda Calculus Base Cases

- Logical constant
- Variable
- Literal
- Lambda term

## Lambda Calculus Logical Constants

- Represent objects in the world

*NYC, CA, RAINIER, LEFT, ...*  
*located\_in, depart\_date, ...*

## Lambda Calculus Variables

- Abstract over objects in the world
- Exact value not pre-determined

*x, y, z, ...*

## Lambda Calculus Literals

- Represent function application

*city(AUSTIN)*  
*located\_in(AUSTIN, TEXAS)*

## Lambda Calculus Literals

- Represent function application

*city(AUSTIN)*  
*located\_in(AUSTIN, TEXAS)*

**Predicate**      **Arguments**

Logical expression      List of logical expressions

## Lambda Calculus Lambda Terms

- Bind/scope a variable
- Repeat to bind multiple variables

$\lambda x. \lambda y. \text{located\_in}(x, y)$

**Lambda operator**      **Variable**      **Body**

## Lambda Calculus Quantifiers?

- Higher order constants
- No need for any special mechanics
- Can represent all of first order logic

$\forall (\lambda x. \text{big}(x) \wedge \text{apple}(x))$   
 $\neg (\exists (\lambda x. \text{lovely}(x)))$   
 $\iota (\lambda x. \text{beautiful}(x) \wedge \text{grammar}(x))$

## Lambda Calculus

### Syntactic Sugar

$$\wedge (A, \wedge(B, C)) \Leftrightarrow A \wedge B \wedge C$$

$$\vee (A, \vee(B, C)) \Leftrightarrow A \vee B \vee C$$

$$\neg(A) \Leftrightarrow \neg A$$

$$Q(\lambda x.f(x)) \Leftrightarrow Qx.f(x)$$

for  $Q \in \{\iota, \mathcal{A}, \exists, \forall\}$

## Simply Typed Lambda Calculus

- Like lambda calculus
- But, typed

✗  $\lambda x.flight(x) \wedge to(x, move)$

✓  $\lambda x.flight(x) \wedge to(x, NYC)$

✗  $\lambda x.NYC(x) \wedge x(to, move)$

[Church 1940]

## Lambda Calculus

### Typing

$t$  Truth-value  
 $e$  Entity

- Simple types
- Complex types

$\langle e, t \rangle$

Type constructor

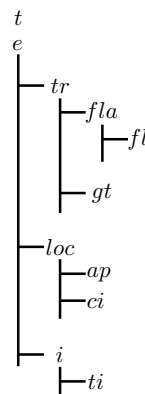
$\langle \langle e, t \rangle, e \rangle$

Domain

Range

## Lambda Calculus

### Typing



- Simple types
- Complex types

$\langle e, t \rangle$

Type constructor

$\langle \langle e, t \rangle, e \rangle$

Domain

Range

- Hierarchical typing system

## Simply Typed Lambda Calculus

$\lambda a.move(a) \wedge dir(a, LEFT) \wedge to(a, ty.chair(y)) \wedge$   
 $pass(a, Ay.sofa(y) \wedge intersect(Az.intersection(z), y))$

Type information usually omitted

## Capturing Meaning with Lambda Calculus

State		
Abbr.	Capital	Pop.
AL	Montgomery	3.9
AK	Juneau	0.4
AZ	Phoenix	2.7

Border	
State1	State2
WA	OR
WA	ID
CA	OR
CA	NV
CA	AZ

Mountains	
Name	State
Bianca	CO
Antero	CO
Rainier	WA
Shasta	CA
Wrangell	AK

Show me mountains in states bordering Texas



[Zettlemoyer and Collins 2005]

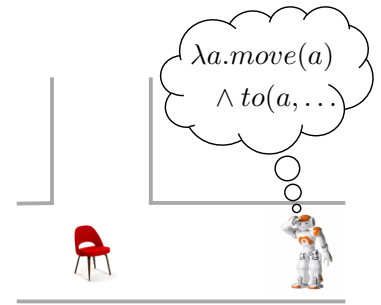
## Capturing Meaning with Lambda Calculus

**SYSTEM** how can I help you ?  
**USER** i ' d like to fly to new york  
**SYSTEM** flying to new york . leaving what city ?  
**USER** from boston on june seven with american airlines  
**SYSTEM** flying to new york . what date would you like to depart boston ?  
**USER** june seventh  
**SYSTEM** do you have a preferred airline ?  
**USER** american airlines  
**SYSTEM** o . k . leaving boston to new york on june seventh flying with american airlines . where would you like to go to next ?  
**USER** back to boston on june tenth  
[CONVERSATION CONTINUES]

[Artzi and Zettlemoyer 2011]

## Capturing Meaning with Lambda Calculus

go to the chair  
and turn right



[Artzi and Zettlemoyer 2013b]

## Capturing Meaning with Lambda Calculus

- Flexible representation
- Can capture full complexity of natural language

More on modeling meaning later

## Constructing Lambda Calculus Expressions

at the chair, move forward three steps past the sofa



$\lambda a. pre(a, \lambda x. chair(x)) \wedge move(a) \wedge len(a, 3) \wedge$   
 $dir(a, forward) \wedge past(a, \lambda y. sofa(y))$

## Combinatory Categorial Grammars

$$\begin{array}{c}
 \frac{CCG \quad \frac{\frac{NP \quad is}{S \backslash NP / ADJ} \quad \frac{fun}{ADJ}}{\lambda f. \lambda x. f(x)} \quad \frac{fun}{ADJ}}{\lambda x. fun(x)} \quad > \\
 \frac{S \backslash NP}{\lambda x. fun(x)} \quad < \\
 \hline
 S \\
 fun(CCG)
 \end{array}$$

[Steedman 1996, 2000]

## Combinatory Categorial Grammars

- Categorical formalism
- Transparent interface between syntax and semantics
- Designed with computation in mind
- Part of a class of mildly context sensitive formalisms (e.g., TAG, HG, LIG) [Joshi et al. 1990]

## CCG Categories

$ADJ : \lambda x. fun(x)$

- Basic building block
- Capture syntactic and semantic information jointly

## CCG Categories

Syntax  $ADJ : \lambda x. fun(x)$  Semantics

- Basic building block
- Capture syntactic and semantic information jointly

## CCG Categories

Syntax  $ADJ : \lambda x. fun(x)$

$(S \backslash NP) / ADJ : \lambda f. \lambda x. f(x)$

$NP : CCG$

- Primitive symbols: N, S, NP, ADJ and PP
- Syntactic combination operator ( $/, \backslash$ )
- Slashes specify argument order and direction

## CCG Categories

$ADJ : \lambda x. fun(x)$  Semantics

$(S \backslash NP) / ADJ : \lambda f. \lambda x. f(x)$

$NP : CCG$

- $\lambda$ -calculus expression
- Syntactic type maps to semantic type

## CCG Lexical Entries

$fun \vdash ADJ : \lambda x. fun(x)$

- Pair words and phrases with meaning
- Meaning captured by a CCG category

## CCG Lexical Entries

fun  $\vdash$   $ADJ : \lambda x. fun(x)$   
Natural Language CCG Category

- Pair words and phrases with meaning
- Meaning captured by a CCG category



## CCG Lexicons

$\text{fun} \vdash \text{ADJ} : \lambda x. \text{fun}(x)$   
 $\text{is} \vdash (S \setminus NP) / \text{ADJ} : \lambda f. \lambda x. f(x)$   
 $\text{CCG} \vdash NP : \text{CCG}$

- Pair words and phrases with meaning
- Meaning captured by a CCG category

## Between CCGs and CFGs

	CFGs	CCGs
Combination operations	Many	Few
Parse tree nodes	Non-terminals	Categories
Syntactic symbols	Few dozen	Handful, but can combine
Paired with words	POS tags	Categories

## Parsing with CCGs

$\text{CCG}$	$\text{is}$	$\text{fun}$
$\frac{NP}{CCG}$	$\frac{S \setminus NP / \text{ADJ}}{\lambda f. \lambda x. f(x)}$	$\frac{\text{ADJ}}{\lambda x. \text{fun}(x)}$

Use lexicon to match words and phrases with their categories

## CCG Operations

- Small set of operators
- Input: 1-2 CCG categories
- Output: A single CCG category
- Operate on syntax semantics together
- Mirror natural logic operations

## CCG Operations Application

$B : g \quad A \setminus B : f \Rightarrow A : f(g) \quad (<)$

$A / B : f \quad B : g \Rightarrow A : f(g) \quad (>)$

- Equivalent to function application
- Two directions: forward and backward
- Determined by slash direction

## CCG Operations Application

<span style="background-color: #90EE90; border: 1px solid black; padding: 2px;">Argument</span>	<span style="background-color: #FF6347; border: 1px solid black; padding: 2px;">Function</span>	<span style="background-color: #6495ED; border: 1px solid black; padding: 2px;">Result</span>
<span style="border: 1px solid black; padding: 5px;"><math>B : g</math></span>	<span style="border: 1px solid black; padding: 5px;"><math>A \setminus B : f</math></span>	$\Rightarrow$ <span style="border: 1px solid black; padding: 5px;"><math>A : f(g)</math></span>

$A / B : f \quad B : g \Rightarrow A : f(g) \quad (>)$

- Equivalent to function application
- Two directions: forward and backward
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## Parsing with CCGs

CCG	is	fun
$\frac{NP}{CCG}$	$\frac{S \backslash NP / ADJ}{\lambda f. \lambda x. f(x)}$	$\frac{ADJ}{\lambda x. fun(x)}$

Use lexicon to match words and phrases with their categories

## Parsing with CCGs

CCG	is	fun
$\frac{NP}{CCG}$	$\frac{S \backslash NP / ADJ}{\lambda f. \lambda x. f(x)}$	$\frac{ADJ}{\lambda x. fun(x)}$
$\frac{S \backslash NP}{\lambda x. fun(x)}$		

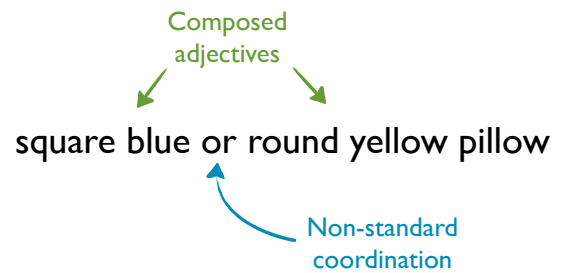
Combine categories using operators  
 $A/B : f \quad B : g \Rightarrow A : f(g) \quad (>)$

## Parsing with CCGs

CCG	is	fun
$\frac{NP}{CCG}$	$\frac{S \backslash NP / ADJ}{\lambda f. \lambda x. f(x)}$	$\frac{ADJ}{\lambda x. fun(x)}$
$\frac{S \backslash NP}{\lambda x. fun(x)}$		
$\frac{S}{fun(CCG)}$		

Combine categories using operators  
 $B : g \quad A \backslash B : f \Rightarrow A : f(g) \quad (<)$

## Parsing with CCGs



## CCG Operations Composition

$$A/B : f \quad B/C : g \Rightarrow A/C : \lambda x. f(g(x)) \quad (> B)$$

$$B \backslash C : g \quad A \backslash B : f \Rightarrow A \backslash C : \lambda x. f(g(x)) \quad (< B)$$

- Equivalent to function composition\*
- Two directions: forward and backward

\* Formal definition of logical composition in supplementary slides

## CCG Operations Composition

$f$	$g$	$f \circ g$
$A/B : f$	$B/C : g$	$A/C : \lambda x. f(g(x))$

$$B \backslash C : g \quad A \backslash B : f \Rightarrow A \backslash C : \lambda x. f(g(x)) \quad (< B)$$

- Equivalent to function composition\*
- Two directions: forward and backward

\* Formal definition of logical composition in supplementary slides

## CCG Operations Type Shifting

Input  $ADJ : \lambda x.g(x)$   $\Rightarrow$  Output  $N/N : \lambda f.\lambda x.f(x) \wedge g(x)$

$PP : \lambda x.g(x) \Rightarrow N \setminus N : \lambda f.\lambda x.f(x) \wedge g(x)$

$AP : \lambda e.g(e) \Rightarrow S \setminus S : \lambda f.\lambda e.f(e) \wedge g(e)$

Topicalization  $AP : \lambda e.g(e) \Rightarrow S/S : \lambda f.\lambda e.f(e) \wedge g(e)$

- Category-specific unary operations
- Modify category type to take an argument
- Helps in keeping a compact lexicon

## CCG Operations Coordination

and  $\vdash C : conj$

or  $\vdash C : disj$

- Coordination is special cased
  - Specific rules perform coordination
  - Coordinating operators are marked with special lexical entries

## Parsing with CCGs

square                  blue                  or                  round                  yellow                  pillow

## Parsing with CCGs

$\frac{\text{square}}{ADJ}$      $\frac{\text{blue}}{ADJ}$      $\frac{\text{or}}{C}$      $\frac{\text{round}}{ADJ}$      $\frac{\text{yellow}}{ADJ}$      $\frac{\text{pillow}}{N}$   
 $\lambda x.square(x)$      $\lambda x.blue(x)$      $disj$      $\lambda x.round(x)$      $\lambda x.yellow(x)$      $\lambda x.pillow(x)$

Use lexicon to match words and phrases with their categories

## Parsing with CCGs

$\frac{\text{square}}{ADJ}$      $\frac{\text{blue}}{ADJ}$      $\frac{\text{or}}{C}$      $\frac{\text{round}}{ADJ}$      $\frac{\text{yellow}}{ADJ}$      $\frac{\text{pillow}}{N}$   
 $\lambda x.square(x)$      $\lambda x.blue(x)$      $disj$      $\lambda x.round(x)$      $\lambda x.yellow(x)$      $\lambda x.pillow(x)$   
 $\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x)}$

Shift adjectives to combine

$ADJ : \lambda x.g(x) \Rightarrow N/N : \lambda f.\lambda x.f(x) \wedge g(x)$

## Parsing with CCGs

$\frac{\text{square}}{ADJ}$      $\frac{\text{blue}}{ADJ}$      $\frac{\text{or}}{C}$      $\frac{\text{round}}{ADJ}$      $\frac{\text{yellow}}{ADJ}$      $\frac{\text{pillow}}{N}$   
 $\lambda x.square(x)$      $\lambda x.blue(x)$      $disj$      $\lambda x.round(x)$      $\lambda x.yellow(x)$      $\lambda x.pillow(x)$   
 $\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x)}$      $\frac{N/N}{\lambda f.\lambda x.f(x) \wedge blue(x)}$      $\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x)}$      $\frac{N/N}{\lambda f.\lambda x.f(x) \wedge yellow(x)}$

Shift adjectives to combine

$ADJ : \lambda x.g(x) \Rightarrow N/N : \lambda f.\lambda x.f(x) \wedge g(x)$

## Parsing with CCGs

square	blue	or	round	yellow	pillow
$\frac{ADJ}{\lambda x.square(x)}$	$\frac{ADJ}{\lambda x.blue(x)}$	$\frac{C}{disj}$	$\frac{ADJ}{\lambda x.round(x)}$	$\frac{ADJ}{\lambda x.yellow(x)}$	$\frac{N}{\lambda x.pillow(x)}$
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge blue(x)}$		$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge yellow(x)}$	
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x) \wedge blue(x)}$			$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x) \wedge yellow(x)}$		

Compose pairs of adjectives

$$A/B : f \quad B/C : g \Rightarrow A/C : \lambda x.f(g(x)) \quad (> B)$$

## Parsing with CCGs

square	blue	or	round	yellow	pillow
$\frac{ADJ}{\lambda x.square(x)}$	$\frac{ADJ}{\lambda x.blue(x)}$	$\frac{C}{disj}$	$\frac{ADJ}{\lambda x.round(x)}$	$\frac{ADJ}{\lambda x.yellow(x)}$	$\frac{N}{\lambda x.pillow(x)}$
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge blue(x)}$		$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge yellow(x)}$	
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x) \wedge blue(x)}$			$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x) \wedge yellow(x)}$		
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge ((square(x) \wedge blue(x)) \vee (round(x) \wedge yellow(x)))}$					

Coordinate composed adjectives

## Parsing with CCGs

square	blue	or	round	yellow	pillow
$\frac{ADJ}{\lambda x.square(x)}$	$\frac{ADJ}{\lambda x.blue(x)}$	$\frac{C}{disj}$	$\frac{ADJ}{\lambda x.round(x)}$	$\frac{ADJ}{\lambda x.yellow(x)}$	$\frac{N}{\lambda x.pillow(x)}$
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge blue(x)}$		$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x)}$	$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge yellow(x)}$	
$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge square(x) \wedge blue(x)}$			$\frac{N/N}{\lambda f.\lambda x.f(x) \wedge round(x) \wedge yellow(x)}$		
$\frac{N/N}{\lambda x.pillow(x) \wedge ((square(x) \wedge blue(x)) \vee (round(x) \wedge yellow(x)))}$					

Apply coordinated adjectives to noun

$$A/B : f \quad B : g \Rightarrow A : f(g) \quad (>)$$

## Parsing with CCGs

$\mathcal{X}$	CCG	is	fun
$\mathcal{Y}$	$\frac{NP}{CCG}$	$\frac{S \setminus NP / ADJ}{\lambda f.\lambda x.f(x)}$	$\frac{ADJ}{\lambda x.fun(x)}$
	$\frac{S \setminus NP}{\lambda x.fun(x)}$		
	$\mathcal{Z} \frac{S}{fun(CCG)}$		

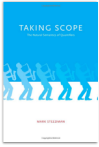
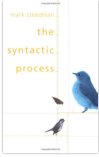


## Weighted Linear CCGs

- Given a weighted linear model:
  - CCG lexicon  $\mathcal{A}$
  - Feature function  $f : X \times Y \rightarrow \mathbb{R}^m$
  - Weights  $w \in \mathbb{R}^m$
- The best parse is:
 
$$y^* = \arg \max_y w \cdot f(x, y)$$
- We consider all possible parses  $y$  for sentence  $x$  given the lexicon  $\mathcal{A}$

## Parsing Algorithms

- Syntax-only CCG parsing has polynomial time CKY-style algorithms
- Parsing with semantics requires entire category as chart signature
  - e.g.,  $ADJ : \lambda x.fun(x)$
- In practice, prune to top-N for each span
  - Approximate, but polynomial time



## More on CCGs

- Generalized type-raising operations
- Cross composition operations for cross serial dependencies
- Compositional approaches to English intonation
- and a lot more ... even Jazz

[Steedman 1996; 2000; 2011; Granroth and Steedman 2012]

## The Lexicon Problem

- Key component of CCG
- Same words often paired with many different categories
- Difficult to learn with limited data

## Factored Lexicons

the house dog      house  $\vdash ADJ : \lambda x.of(x, \iota y.house(y))$

the dog of the house      house  $\vdash N : \lambda x.house(x)$   
 $\iota x.dog(x) \wedge of(x, \iota y.house(y))$

the garden dog      garden  $\vdash ADJ : \lambda x.of(x, \iota y.garden(y))$   
 $\iota x.dog(x) \wedge of(x, \iota y.garden(y))$

- Lexical entries share information
- Decomposition of entries can lead to more compact lexicons

## Factored Lexicons

the house dog      house  $\vdash ADJ : \lambda x.of(x, \iota y.house(y))$

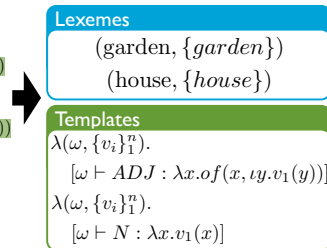
the dog of the house      house  $\vdash N : \lambda x.house(x)$   
 $\iota x.dog(x) \wedge of(x, \iota y.house(y))$

the garden dog      garden  $\vdash ADJ : \lambda x.of(x, \iota y.garden(y))$   
 $\iota x.dog(x) \wedge of(x, \iota y.garden(y))$

- Lexical entries share information
- Decomposition of entries can lead to more compact lexicons

## Factored Lexicons

house  $\vdash ADJ : \lambda x.of(x, \iota y.house(y))$   
house  $\vdash N : \lambda x.house(x)$   
garden  $\vdash ADJ : \lambda x.of(x, \iota y.garden(y))$



## Factored Lexicons

Templates

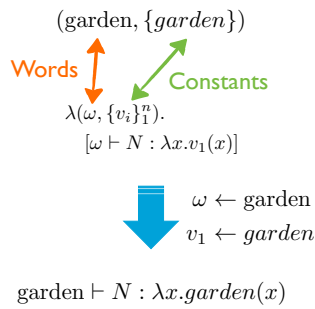
- $\lambda(\omega, \{v_i\}_1^n).$   
[ $\omega \vdash ADJ : \lambda x.of(x, \iota y.v_1(y))$ ]
- $\lambda(\omega, \{v_i\}_1^n).$   
[ $\omega \vdash N : \lambda x.v_1(x)$ ]

Lexemes

- (garden, {garden})
- (house, {house})

- Capture systematic variations in word usage
- Each variation can then be applied to compact units of lexical meaning
- Model word meaning
- Abstracts the compositional nature of the word

## Factored Lexicons



## Factored Lexicons

Original Lexicon	$\text{flight} \vdash S NP : \lambda x.\text{flight}(x)$ $\text{flight} \vdash S NP/(S NP) : \lambda f.\lambda x.\text{flight}(x) \wedge f(x)$ $\text{flight} \vdash S NP \setminus (S NP) : \lambda f.\lambda x.\text{flight}(x) \wedge f(x)$ $\text{ground transport} \vdash S NP : \lambda x.\text{trans}(x)$ $\text{ground transport} \vdash S NP/(S NP) : \lambda f.\lambda x.\text{trans}(x) \wedge f(x)$ $\text{ground transport} \vdash S NP \setminus (S NP) : \lambda f.\lambda x.\text{trans}(x) \wedge f(x)$
Factored Lexicon	$(\text{flight}, \{\text{flight}\})$ $(\text{ground transport}, \{\text{trans}\})$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash S NP : \lambda x.v_1(x)]$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash S NP/(S NP) : \lambda f.\lambda x.v_1(x) \wedge f(x)]$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash S NP \setminus (S NP) : \lambda f.\lambda x.v_1(x) \wedge f(x)]$

## Factoring a Lexical Entry

$\text{house} \vdash ADJ : \lambda x.of(x, \iota y.\text{house}(y))$

Partial factoring	$(\text{house}, \{\text{house}\})$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash ADJ : \lambda x.of(x, \iota y.v_1(y))]$
Partial factoring	$(\text{house}, \{\text{of}\})$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash ADJ : \lambda x.v_1(x, \iota y.\text{house}(y))]$
Maximal factoring	$(\text{house}, \{\text{of}, \text{house}\})$ $\lambda(\omega, \{v_i\}_1^n).[\omega \vdash ADJ : \lambda x.v_1(x, \iota y.v_2(y))]$

Parsing

Learning

Modeling

- Lambda calculus
- Parsing with Combinatory Categorical Grammars
- Linear CCGs
- Factored lexicons

## Learning

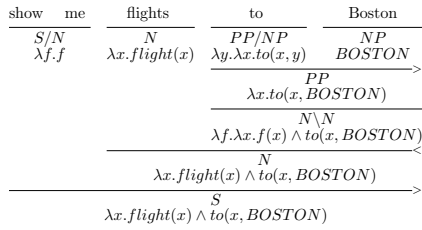


- What kind of data/supervision we can use?
- What do we need to learn?

## Parsing as Structure Prediction

show	me	flights	to	Boston
$S N$	$N$	$PP NP$	$NP$	$BOSTON$
$\lambda f.f$	$\lambda x.\text{flight}(x)$	$\lambda y.\lambda x.\text{to}(x, y)$	$\lambda y.\lambda x.\text{to}(x, y)$	$\lambda y.\lambda x.\text{to}(x, y)$
$\lambda x.\text{to}(x, BOSTON)$				
$\lambda f.\lambda x.f(x) \wedge \text{to}(x, BOSTON)$				
$\lambda x.\text{flight}(x) \wedge \text{to}(x, BOSTON)$				
$\lambda x.\text{flight}(x) \wedge \text{to}(x, BOSTON)$				

## Learning CCG

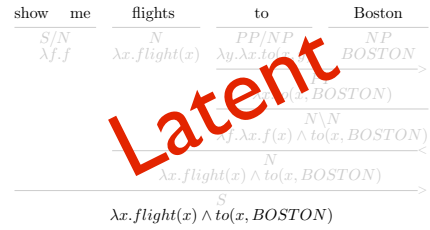


Lexicon

Combinators  
Predefined

$w$

## Supervised Data



Latent

## Supervised Data

Supervised learning is done from pairs of sentences and logical forms

Show me flights to Boston  
 $\lambda x.flight(x) \wedge to(x, BOSTON)$

I need a flight from baltimore to seattle  
 $\lambda x.flight(x) \wedge from(x, BALTIMORE) \wedge to(x, SEATTLE)$

what ground transportation is available in san francisco  
 $\lambda x.ground\_transport(x) \wedge to.city(x, SF)$

[Zettlemoyer and Collins 2005; 2007]

## Weak Supervision

- Logical form is latent
- “Labeling” requires less expertise
- Labels don’t uniquely determine correct logical forms
- Learning requires executing logical forms within a system and evaluating the result

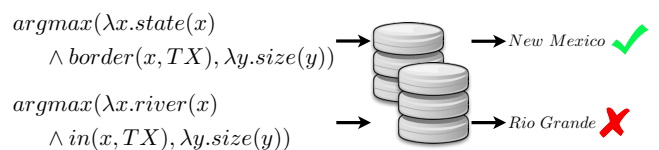
## Weak Supervision Learning from Query Answers

What is the largest state that borders Texas?  
*New Mexico*

[Clarke et al. 2010; Liang et al. 2011]

## Weak Supervision Learning from Query Answers

What is the largest state that borders Texas?  
*New Mexico*



[Clarke et al. 2010; Liang et al. 2011]

## Weak Supervision Learning from Demonstrations

at the chair, move forward three steps past the sofa



Some examples from other domains:

- Sentences and labeled game states [Goldwasser and Roth 2011]
- Sentences and sets of physical objects [Matuszek et al. 2012]

[Chen and Mooney 2011; Kim and Mooney 2012; Artzi and Zettlemoyer 2013b]

## Weak Supervision Learning from Conversation Logs

**SYSTEM** how can I help you ? (OPEN\_TASK)  
**USER** i ' d like to fly to new york  
**SYSTEM** flying to new york . (CONFIRM: from(f, ATL)) leaving what city ? (ASK: λx.from(f,x))  
**USER** from boston on june seven with american airlines  
**SYSTEM** flying to new york . (CONFIRM: to(f, NYC)) what date would you like to depart boston ? (ASK: λx.date(f,x)^to(f, BOS))  
**USER** june seventh  
[CONVERSATION CONTINUES]

[Artzi and Zettlemoyer 2011]

Parsing

Learning

Modeling

- Structured perceptron
- A unified learning algorithm
- Supervised learning
- Weak supervision

## Structured Perceptron

- Simple additive updates
  - Only requires efficient decoding (argmax)
  - Closely related to MaxEnt and other feature rich models
  - Provably finds linear separator in finite updates, if one exists
- Challenge: learning with hidden variables

## Structured Perceptron

**Data:**  $\{(x_i, y_i) : i = 1 \dots n\}$

For  $t = 1 \dots T$ : [iterate epochs]

For  $i = 1 \dots n$ : [iterate examples]

$y^* \leftarrow \arg \max_y \langle \theta, \Phi(x_i, y) \rangle$  [predict]

If  $y^* \neq y_i$ : [check]

$\theta \leftarrow \theta + \Phi(x_i, y_i) - \Phi(x_i, y^*)$  [update]

[Collins 2002]

## One Derivation of the Perceptron

**Log-linear model:**  $p(y|x) = \frac{e^{w \cdot f(x,y)}}{\sum_{y'} e^{w \cdot f(x,y')}}$

Step 1: Differentiate, to maximize data log-likelihood

$$update = \sum_i f(x_i, y_i) - E_{p(y|x_i)} f(x_i, y)$$

Step 2: Use online, stochastic gradient updates, for example  $i$ :

$$update_i = f(x_i, y_i) - E_{p(y|x_i)} f(x_i, y)$$

Step 3: Replace expectations with maxes (Viterbi approx.)

$$update_i = f(x_i, y_i) - f(x_i, y^*) \text{ where } y^* = \arg \max_y w \cdot f(x_i, y)$$



## The Perceptron with Hidden Variables

Log-linear  
**model:**  $p(y|x) = \sum_h p(y, h|x) \quad p(y, h|x) = \frac{e^{w \cdot f(x, h, y)}}{\sum_{y', h'} e^{w \cdot f(x, h', y')}}$

Step 1: Differentiate marginal, to maximize data log-likelihood

$$\text{update} = \sum_i E_{p(h|y_i, x_i)}[f(x_i, h, y_i)] - E_{p(y, h|x_i)}[f(x_i, h, y)]$$

Step 2: Use online, stochastic gradient updates, for example  $i$ :

$$\text{update}_i = E_{p(y_i, h|x_i)}[f(x_i, h, y_i)] - E_{p(y, h|x_i)}[f(x_i, h, y)]$$

Step 3: Replace expectations with maxes (Viterbi approx.)

$$\text{update}_i = f(x_i, h', y_i) - f(x_i, h^*, y^*) \text{ where}$$

$$y^*, h^* = \arg \max_{y, h} w \cdot f(x_i, h, y) \text{ and } h' = \arg \max_h w \cdot f(x_i, h, y_i)$$

## Hidden Variable Perceptron

**Data:**  $\{(x_i, y_i) : i = 1 \dots n\}$

For  $t = 1 \dots T$ :

[iterate epochs]

For  $i = 1 \dots n$ :

[iterate examples]

$$y^*, h^* \leftarrow \arg \max_{y, h} \langle \theta, \Phi(x_i, h, y) \rangle \quad \text{[predict]}$$

If  $y^* \neq y_i$ : [check]

$$h' \leftarrow \arg \max_h \langle \theta, \Phi(x_i, h, y_i) \rangle \quad \text{[predict hidden]}$$

$$\theta \leftarrow \theta + \Phi(x_i, h', y_i) - \Phi(x_i, h^*, y^*) \quad \text{[update]}$$

[Liang et al. 2006; Zettlemoyer and Collins 2007]

## Hidden Variable Perceptron

- No known convergence guarantees
  - Log-linear version is non-convex
- Simple and easy to implement
  - Works well with careful initialization
- Modifications for semantic parsing
  - Lots of different hidden information
  - Can add a margin constraint, do probabilistic version, etc.

## Unified Learning Algorithm

- Handle various learning signals
- Estimate parsing parameters
- Induce lexicon structure
- Related to loss-sensitive structured perceptron [Singh-Miller and Collins 2007]

## Learning Choices

### Validation Function

$$\mathcal{V} : \mathcal{Y} \rightarrow \{t, f\}$$

- Indicates correctness of a parse  $y$
- Varying  $\mathcal{V}$  allows for differing forms of supervision

### Lexical Generation Procedure

$$\text{GENLEX}(x, \mathcal{V}; \Lambda, \theta)$$

- Given:
  - sentence  $x$
  - validation function  $\mathcal{V}$
  - lexicon  $\Lambda$
  - parameters  $\theta$
- Produce a overly general set of lexical entries

## Unified Learning Algorithm

Initialize  $\theta$  using  $\Lambda_0, \Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

Step 1: (Lexical generation)

Step 2: (Update parameters)

Output: Parameters  $\theta$  and lexicon  $\Lambda$

- Online
- Input:  $\{(x_i, \mathcal{V}_i) : i = 1 \dots n\}$
- 2 steps:
  - Lexical generation
  - Parameter update

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

**Initialize parameters and lexicon**

$\theta$  weights  
 $\Lambda_0$  initial lexicon

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

**Iterate over data**

$T$  # iterations  
 $n$  # samples

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

- Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$
- Select lexical entries from the highest scoring valid parses:  
 $\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$
- Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

- Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
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 $\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$
- Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

**Generate a large set of potential lexical entries**

$\theta$  weights  
 $x_i$  sentence  
 $\mathcal{V}_i$  validation function  
 $GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$   
lexical generation function

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

- Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$
- Select lexical entries from the highest scoring valid parses:  
 $\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$
- Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

**Generate a large set of potential lexical entries**

$\theta$  weights  
 $x_i$  sentence  
 $\mathcal{V}_i$  validation function  
 $GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$   
lexical generation function

**Procedure to propose potential new lexical entries for a sentence**

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

- Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$
- Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$
- Select lexical entries from the highest scoring valid parses:  
 $\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$
- Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

**Generate a large set of potential lexical entries**

$\theta$  weights  
 $x_i$  sentence  
 $\mathcal{V}_i$  validation function  
 $GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$   
lexical generation function

$\mathcal{V} : \mathcal{Y} \rightarrow \{t, f\}$   
 $\mathcal{Y}$  all parses

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

a. Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$

b. Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$

c. Select lexical entries from the highest scoring valid parses:

$$\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$$

d. Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Get top parses

$x_i$  sentence  
 $k$  beam size  
 $GEN(x_i; \lambda)$  set of all parses

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

a. Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$

b. Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$

c. Select lexical entries from the highest scoring valid parses:

$$\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$$

d. Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Get lexical entries from highest scoring valid parses

$\theta$  weights  
 $\mathcal{V}$  validation function  
 $LEX(y)$  set of lexical entries  
 $\phi_i(y) = \phi(x_i, y)$   
 $MAXV_i(Y; \theta) = \{y | y \in Y \wedge \mathcal{V}_i(y) \wedge \forall y' \in Y. \mathcal{V}_i(y) \implies \langle \theta, \Phi_i(y') \rangle \leq \langle \theta, \Phi_i(y) \rangle\}$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

a. Set  $\lambda_G \leftarrow GENLEX(x_i, \mathcal{V}_i; \Lambda, \theta)$ ,  
 $\lambda \leftarrow \Lambda \cup \lambda_G$

b. Let  $Y$  be the  $k$  highest scoring parses from  $GEN(x_i; \lambda)$

c. Select lexical entries from the highest scoring valid parses:

$$\lambda_i \leftarrow \bigcup_{y \in MAXV_i(Y; \theta)} LEX(y)$$

d. Update lexicon:  $\Lambda \leftarrow \Lambda \cup \lambda_i$

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Update model's lexicon

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

a. Set  $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$   
and  $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$

b. Construct sets of margin violating good and bad parses:

$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i \text{ s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

$$E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i \text{ s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

c. Apply the additive update:

$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r) - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

a. Set  $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$   
and  $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$

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c. Apply the additive update:

$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r) - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Re-parse and group all parses into 'good' and 'bad' sets

$\theta$  weights  
 $x_i$  sentence  
 $\mathcal{V}_i$  validation function  
 $GEN(x_i; \lambda)$  set of all parses  
 $\phi_i(y) = \phi(x_i, y)$   
 $MAXV_i(Y; \theta) = \{y | y \in Y \wedge \mathcal{V}_i(y) \wedge \forall y' \in Y. \mathcal{V}_i(y) \implies \langle \theta, \Phi_i(y') \rangle \leq \langle \theta, \Phi_i(y) \rangle\}$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

a. Set  $G_i \leftarrow MAXV_i(GEN(x_i; \Lambda); \theta)$   
and  $B_i \leftarrow \{e | e \in GEN(x_i; \Lambda) \wedge \neg \mathcal{V}_i(y)\}$

b. Construct sets of margin violating good and bad parses:

$$R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i \text{ s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

$$E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i \text{ s.t. } \langle \theta, \Phi_i(g) - \Phi_i(b) \rangle < \gamma \Delta_i(g, b)\}$$

c. Apply the additive update:

$$\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r) - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$$

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

For all pairs of 'good' and 'bad' parses, if their scores violate the margin, add each to 'right' and 'error' sets respectively

$\theta$  weights  
 $\gamma$  margin  
 $\phi_i(y) = \phi(x_i, y)$   
 $\Delta_i(y, y') = |\Phi_i(y) - \Phi_i(y')|_1$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

a. Set  $G_i \leftarrow \text{MAX}_{V_i}(\text{GEN}(x_i; \Lambda); \theta)$   
and  $B_i \leftarrow \{e | e \in \text{GEN}(x_i; \Lambda) \wedge \neg V_i(y)\}$

b. Construct sets of margin violating good and bad parses:  
 $R_i \leftarrow \{g | g \in G_i \wedge \exists b \in B_i$   
 $\quad \text{s.t. } (\theta, \Phi_i(g) - \Phi_i(b)) < \gamma \Delta_i(g, b)\}$   
 $E_i \leftarrow \{b | b \in B_i \wedge \exists g \in G_i$   
 $\quad \text{s.t. } (\theta, \Phi_i(g) - \Phi_i(b)) < \gamma \Delta_i(g, b)\}$

c. Apply the additive update:  
 $\theta \leftarrow \theta + \frac{1}{|R_i|} \sum_{r \in R_i} \Phi_i(r)$   
 $\quad - \frac{1}{|E_i|} \sum_{e \in E_i} \Phi_i(e)$

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Update towards  
violating 'good' parses  
and against violating 'bad'  
parses

$\theta$  weights  
 $\phi_i(y) = \phi(x_i, y)$

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

Return grammar

$\theta$  weights  
 $\Lambda$  lexicon

## Features and Initialization

Feature Classes

- Parse: indicate lexical entry and combinator use
- Logical form: indicate local properties of logical forms, such as constant co-occurrence

Lexicon Initialization

- Often use an NP list
- Sometimes include additional, domain independent entries for function words

Initial Weights

- Positive weight for initial lexical indicator features

## Unified Learning Algorithm

$\mathcal{V}$  validation function  
 $\text{GENLEX}(x, \mathcal{V}; \lambda, \theta)$   
 lexical generation function

- Two parts of the algorithm we still need to define
- Depend on the task and supervision signal

## Unified Learning Algorithm

Supervised

$\mathcal{V}$

Template-based  $\text{GENLEX}$

Unification-based  $\text{GENLEX}$

Weakly Supervised

$\mathcal{V}$

Template-based  $\text{GENLEX}$

## Supervised Learning

show me the afternoon flights from LA to boston

$\lambda x. \text{flight}(x) \wedge \text{during}(x, \text{AFTERNOON}) \wedge \text{from}(x, \text{LA}) \wedge \text{to}(x, \text{BOS})$

Parse structure is latent

## Supervised Learning

Supervised

$\mathcal{V}$

Template-based *GENLEX*

Unification-based *GENLEX*

## Supervised Validation Function

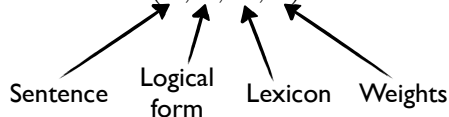
- Validate logical form against gold label

$$\mathcal{V}_i(y) = \begin{cases} true & \text{if } LF(y) = z_i \\ false & \text{else} \end{cases}$$

$y$  parse  
 $z_i$  labeled logical form  
 $LF(y)$  logical form at the root of  $y$

## Supervised Template-based

*GENLEX*( $x, z; \Lambda, \theta$ )



Small notation abuse:  
take labeled logical  
form instead of  
validation function

## Supervised Template-based

*GENLEX*( $x, z; \Lambda, \theta$ )

I want a flight to new york  
 $\lambda x. flight(x) \wedge to(x, NYC)$

## Supervised Template-based GENLEX

- Use templates to constrain lexical entries structure
- For example: from a small annotated dataset

$\lambda(\omega, \{v_i\}_1^n). [\omega \vdash ADJ : \lambda x. v_1(x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash PP : \lambda x. \lambda y. v_1(y, x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash N : \lambda x. v_1(x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash S \setminus NP/NP : \lambda x. \lambda y. v_1(x, y)]$   
 ...

[Zettlemoyer and Collins 2005]

## Supervised Template-based GENLEX

Need lexemes to instantiate templates

$\lambda(\omega, \{v_i\}_1^n). [\omega \vdash ADJ : \lambda x. v_1(x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash PP : \lambda x. \lambda y. v_1(y, x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash N : \lambda x. v_1(x)]$   
 $\lambda(\omega, \{v_i\}_1^n). [\omega \vdash S \setminus NP/NP : \lambda x. \lambda y. v_1(x, y)]$   
 ...

## Supervised Template-based

$GENLEX(x, z; \Lambda, \theta)$

All possible sub-strings

I want a flight to new york  
 $\lambda x.flight(x) \wedge to(x, NYC)$

I want  
 a flight  
 flight  
 flight to new  
 ...

## Supervised Template-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to new york  
 $\lambda x.flight(x) \wedge to(x, NYC)$

All logical constants from labeled logical form

I want  
 a flight  
 flight  
 flight to new  
 ...

*flight*  
*to*  
*NYC*

## Supervised Template-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to new york  
 $\lambda x.flight(x) \wedge to(x, NYC)$

I want  
 a flight  
 flight  
 flight to new  
 ...

~~to~~  
~~NYC~~



(flight, {flight})  
 (I want, {})  
 (flight to new, {to, NYC})  
 ...

Create lexemes

## Supervised Template-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to new york  
 $\lambda x.flight(x) \wedge to(x, NYC)$

I want  
 a flight  
 flight  
 flight to new  
 ...  
 (flight, {flight})  
 (I want, {})  
 (flight to new, {to, NYC})  
 ...

~~to~~  
~~NYC~~

Initialize templates



flight  $\vdash N : \lambda x.flight(x)$   
 I want  $\vdash S/NP : \lambda x.x$   
 flight to new :  $S \setminus NP/NP : \lambda x.\lambda y.to(x, y)$   
 ...

## Fast Parsing with Pruning

- GENLEX outputs a large number of entries
- For fast parsing: use the labeled logical form to prune
- Prune partial logical forms that can't lead to labeled form

I want a flight from New York to Boston on Delta  
 $\lambda x.from(x, NYC) \wedge to(x, BOS) \wedge carrier(x, DL)$

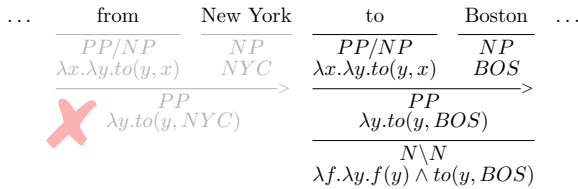
## Fast Parsing with Pruning

I want a flight from New York to Boston on Delta  
 $\lambda x.from(x, NYC) \wedge to(x, BOS) \wedge carrier(x, DL)$

...  $\frac{\frac{PP/NP}{\lambda x.\lambda y.to(y, x)} \quad \frac{NP}{NYC}}{PP} \rightarrow \frac{\frac{PP/NP}{\lambda x.\lambda y.to(y, x)} \quad \frac{NP}{BOS}}{PP} \rightarrow$   
 ~~$\lambda y.to(y, NYC)$~~   $\lambda y.to(y, BOS)$  ...

## Fast Parsing with Pruning

I want a flight from New York to Boston on Delta  
 $\lambda x. \text{from}(x, \text{NYC}) \wedge \text{to}(x, \text{BOS}) \wedge \text{carrier}(x, \text{DL})$



## Supervised Template-based GENLEX

### Summary

No initial expert knowledge	
Creates compact lexicons	✓
Language independent	
Representation independent	
Easily inject linguistic knowledge	✓
Weakly supervised learning	✓

## Unification-based GENLEX

- Automatically learns the templates
  - Can be applied to any language and many different approaches for semantic modeling
- Two step process
  - Initialize lexicon with labeled logical forms
  - "Reverse" parsing operations to split lexical entries

[Kwiatkowski et al. 2010]

## Unification-based GENLEX

- Initialize lexicon with labeled logical forms

For every labeled training example:

I want a flight to Boston  
 $\lambda x. \text{flight}(x) \wedge \text{to}(x, \text{BOS})$

Initialize the lexicon with:

I want a flight to Boston  $\vdash S : \lambda x. \text{flight}(x) \wedge \text{to}(x, \text{BOS})$

## Unification-based GENLEX

- Splitting lexical entries

I want a flight to Boston  $\vdash S : \lambda x. \text{flight}(x) \wedge \text{to}(x, \text{BOS})$



I want a flight  $\vdash S/(S|NP) : \lambda f. \lambda x. \text{flight}(x) \wedge f(x)$   
 to Boston  $\vdash S|NP : \lambda x. \text{to}(x, \text{BOS})$

Many possible phrase pairs ✗

Many possible category pairs

## Unification-based GENLEX

- Splitting CCG categories:

1. Split logical form  $h$  to  $f$  and  $g$  s.t.

$$f(g) = h \text{ or } \lambda x. f(g(x)) = h$$

2. Infer syntax from logical form type

$$\begin{aligned} S/(S|NP) &: \lambda f. \lambda x. \text{flight}(x) \wedge f(x) \\ S|NP &: \lambda x. \text{to}(x, \text{BOS}) \end{aligned}$$

$S : \lambda x. \text{flight}(x) \wedge \text{to}(x, \text{BOS})$   $\rightarrow$

$$\begin{aligned} S|NP &: \lambda y. \lambda x. \text{flight}(x) \wedge f(x, y) \\ NP &: \text{BOS} \end{aligned}$$

...

## Unification-based GENLEX

- Split text and create all pairs

I want a flight to Boston  $\vdash S : \lambda x. flight(x) \wedge to(x, BOS)$



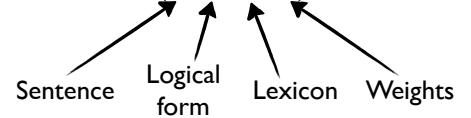
I want  $S/(S|NP) : \lambda f. \lambda x. flight(x) \wedge f(x)$   
 a flight to Boston  $S|NP : \lambda x. to(x, BOS)$

I want a flight  $S/(S|NP) : \lambda f. \lambda x. flight(x) \wedge f(x)$   
 to Boston  $S|NP : \lambda x. to(x, BOS)$

...

## Unification-based

$GENLEX(x, z; \Lambda, \theta)$

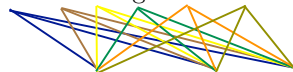


- Find highest scoring correct parse
- Find split that most increases score
- Return new lexical entries

## Parameter Initialization

Compute co-occurrence (IBM Model 1)  
 between words and logical constants

I want a flight to Boston



$S : \lambda x. flight(x) \wedge to(x, BOS)$

Initial score for new lexical entries: average  
 over pairwise weights

## Unification-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston

$\lambda x. flight(x) \wedge to(x, BOS)$

## Unification-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston

$\lambda x. flight(x) \wedge to(x, BOS)$

- Find highest scoring correct parse
- Find splits that most increases score
- Return new lexical entries

I want a flight to Boston

$\frac{S}{\lambda x. flight(x) \wedge to(x, BOS)}$

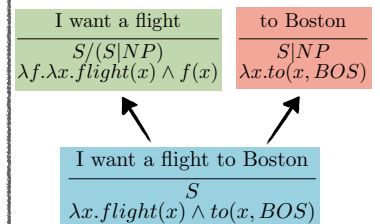
## Unification-based

$GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston

$\lambda x. flight(x) \wedge to(x, BOS)$

- Find highest scoring correct parse
- Find splits that most increases score
- Return new lexical entries

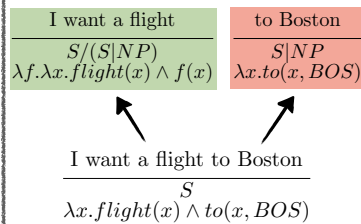




## Unification-based $GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston  
 $\lambda x.flight(x) \wedge to(x, BOS)$

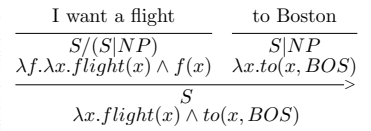
1. Find highest scoring correct parse
2. Find splits that most increases score
3. Return new lexical entries



## Unification-based $GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston  
 $\lambda x.flight(x) \wedge to(x, BOS)$

1. Find highest scoring correct parse
2. Find splits that most increases score
3. Return new lexical entries

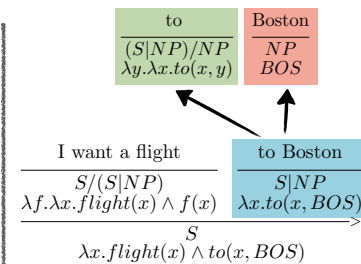


Iteration 2

## Unification-based $GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston  
 $\lambda x.flight(x) \wedge to(x, BOS)$

1. Find highest scoring correct parse
2. Find splits that most increases score
3. Return new lexical entries

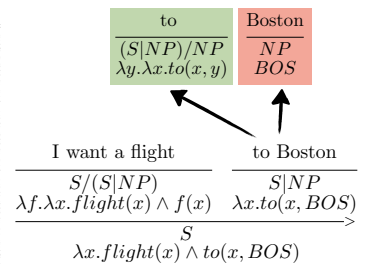


Iteration 2

## Unification-based $GENLEX(x, z; \Lambda, \theta)$

I want a flight to Boston  
 $\lambda x.flight(x) \wedge to(x, BOS)$

1. Find highest scoring correct parse
2. Find splits that most increases score
3. Return new lexical entries



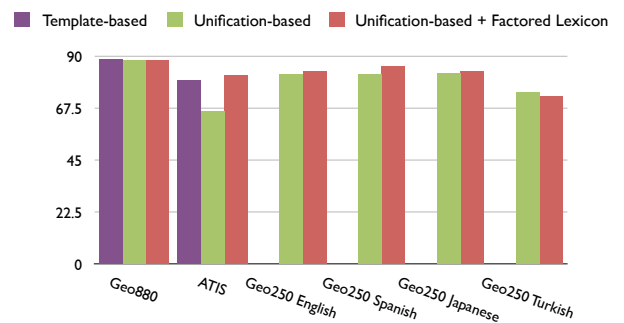
Iteration 2

## Experiments

- Two database corpora:
  - Geo880/Geo250 [Zelle and Mooney 1996; Tang and Mooney 2001]
  - ATIS [Dahl et al. 1994]
- Learning from sentences paired with logical forms
- Comparing template-based and unification-based GENLEX methods

[Zettlemoyer and Collins 2007; Kwiatkowski et al. 2010; 2011]

## Results



[Zettlemoyer and Collins 2007; Kwiatkowski et al. 2010; 2011]

## GENLEX Comparison

	Templates	Unification
No initial expert knowledge		✓
Creates compact lexicons	✓	
Language independent		✓
Representation independent		✓
Easily inject linguistic knowledge	✓	
Weakly supervised learning	✓	?

## Recap CCGs

$$\begin{array}{c}
 \text{CCG} \quad \text{is} \quad \text{fun} \\
 \frac{NP}{CCG} \quad \frac{S \setminus NP / ADJ}{\lambda f. \lambda x. f(x)} \quad \frac{ADJ}{\lambda x. fun(x)} \\
 \hline
 \frac{S \setminus NP}{\lambda x. fun(x)} \\
 \hline
 \frac{S}{fun(CCG)}
 \end{array}$$

[Steedman 1996, 2000]

## Recap Unified Learning Algorithm

Initialize  $\theta$  using  $\Lambda_0$ ,  $\Lambda \leftarrow \Lambda_0$

For  $t = 1 \dots T, i = 1 \dots n$ :

**Step 1:** (Lexical generation)

**Step 2:** (Update parameters)

**Output:** Parameters  $\theta$  and lexicon  $\Lambda$

- Online
- 2 steps:
  - Lexical generation
  - Parameter update

## Recap Learning Choices

Validation Function

$$\mathcal{V} : \mathcal{Y} \rightarrow \{t, f\}$$

- Indicates correctness of a parse  $y$
- Varying  $\mathcal{V}$  allows for differing forms of supervision

Lexical Generation Procedure

$$GENLEX(x, \mathcal{V}; \Lambda, \theta)$$

- Given:
  - sentence  $x$
  - validation function  $\mathcal{V}$
  - lexicon  $\Lambda$
  - parameters  $\theta$
- Produce a overly general set of lexical entries

## Unified Learning Algorithm

Supervised

$\mathcal{V}$

Template-based *GENLEX*

Unification-based *GENLEX*

Weakly Supervised

$\mathcal{V}$

Template-based *GENLEX*

## Weak Supervision

What is the largest state that borders Texas?

New Mexico

[Clarke et al. 2010; Liang et al. 2011]

# Weak Supervision

What is the largest state that borders Texas?

New Mexico

at the chair, move forward three steps past the sofa



Execute the logical form and observe the result

# Weakly Supervised Validation Function

$$\mathcal{V}_i(y) = \begin{cases} true & \text{if } EXEC(y) \approx e_i \\ false & \text{else} \end{cases}$$

$y \in \mathcal{Y}$  parse  
 $e_i \in \mathcal{E}$  available execution result  
 $EXEC(y) : \mathcal{Y} \rightarrow \mathcal{E}$   
 logical form at the root of  $y$

[Arzti and Zettlemoyer 2013b]

# Weakly Supervised Validation Function

$$\mathcal{V}_i(y) = \begin{cases} true & \text{if } EXEC(y) \approx e_i \\ false & \text{else} \end{cases}$$

Depends on supervision

Domain-specific execution function:  
 SQL query engine,  
 navigation robot

$y \in \mathcal{Y}$  parse  
 $e_i \in \mathcal{E}$  available execution result  
 $EXEC(y) : \mathcal{Y} \rightarrow \mathcal{E}$   
 logical form at the root of  $y$

In general: execution function is a natural part of a complete system

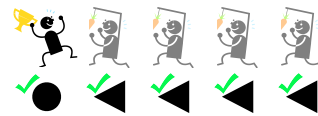
# Weakly Supervised Validation Function

Example  $EXEC(y)$ :

Robot moving in an environment

Example supervision:

Complete Demonstration



Validate all steps



# Weakly Supervised Validation Function

Example  $EXEC(y)$ :

Robot moving in an environment

Example supervision:

Final State



Validate only last position



# Weakly Supervised GENLEX( $x, \mathcal{V}; \Lambda, \theta$ )

I want a flight to new york

~~$\lambda x. flight(x) \wedge to(x, NYC)$~~

I want a flight  
 flight  
 flight to new  
 ...

No access to labeled logical form

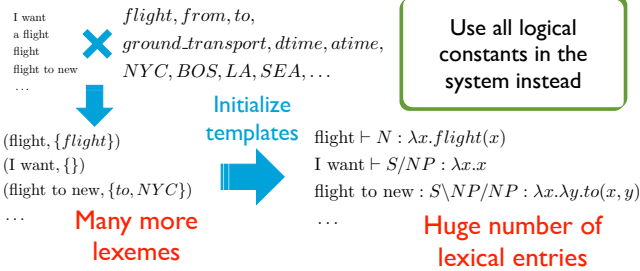
Initialize templates

$(flight, \{flight\})$   
 $(I\ want, \{\})$   
 $(flight\ to\ new, \{to, NYC\})$   
 ...

$flight \vdash N : \lambda x. flight(x)$   
 $I\ want \vdash S/NP : \lambda x.x$   
 $flight\ to\ new : S \setminus NP / NP : \lambda x. \lambda y. to(x, y)$   
 ...

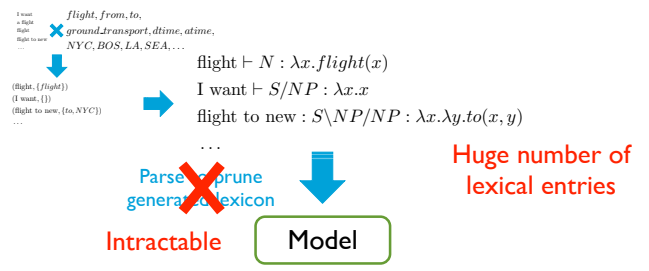
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

I want a flight to new york



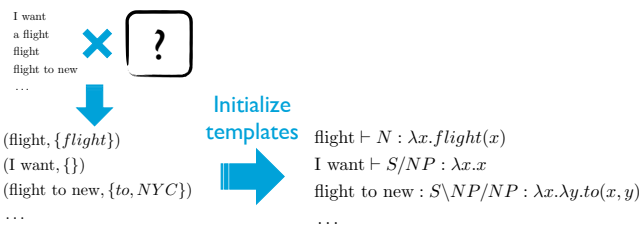
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

I want a flight to new york



## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

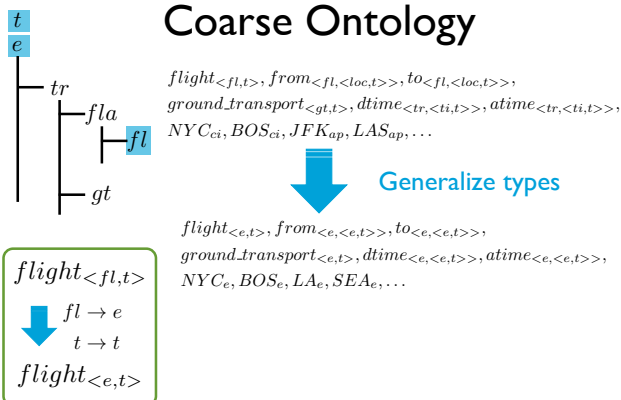
I want a flight to new york



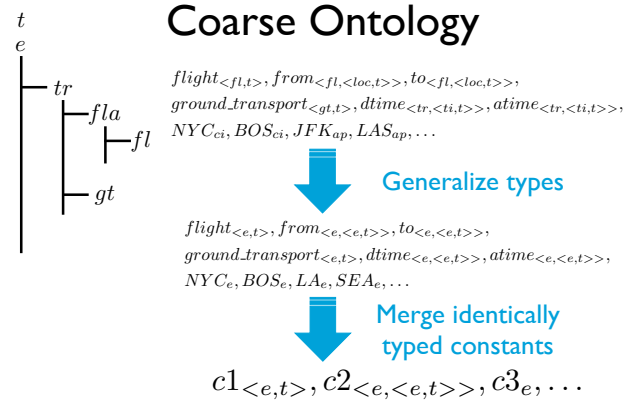
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

- Gradually prune lexical entries using a coarse-to-fine semantic parsing algorithm
- Transition from coarse to fine defined by typing system

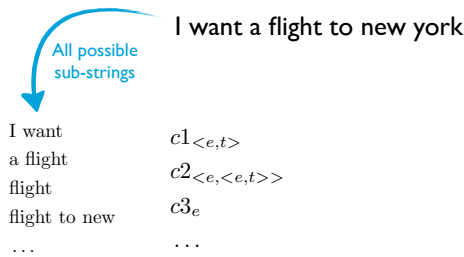
## Coarse Ontology



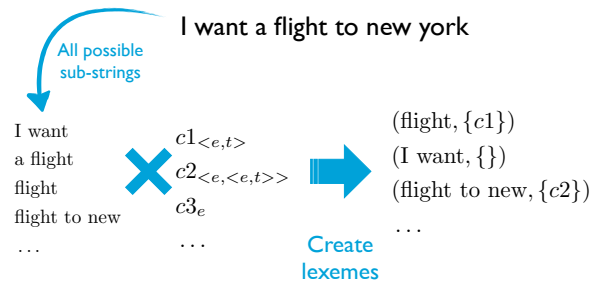
## Coarse Ontology



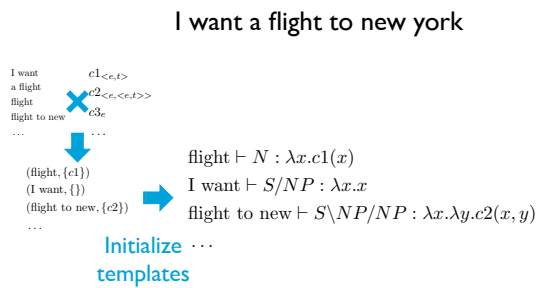
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



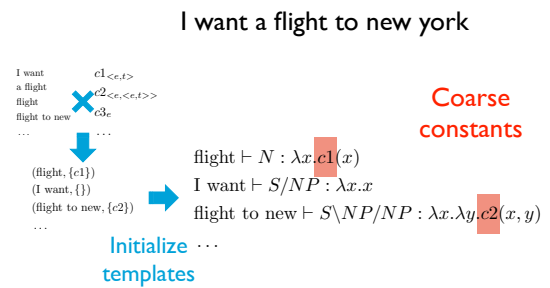
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



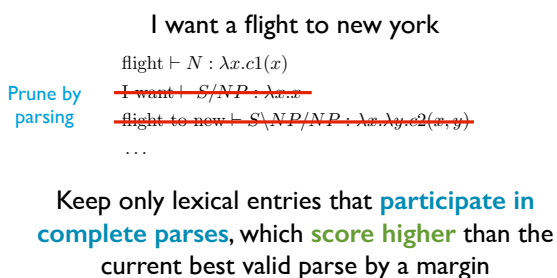
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



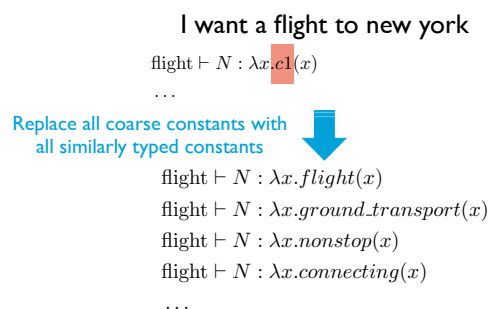
## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



## Weakly Supervised $GENLEX(x, \mathcal{V}; \Lambda, \theta)$



## Weak Supervision Requirements

- Know how to act given a logical form
- A validation function
- Templates for lexical induction

## Experiments

Instruction:

at the chair; move forward three steps past the sofa

Demonstration:



- Situated learning with joint inference
- Two forms of validation
- Template-based  $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

[Artzi and Zettlemoyer 2013b]

## Results



## Unified Learning Algorithm Extensions

- Loss-sensitive learning
  - Applied to learning from conversations
- Stochastic gradient descent
  - Approximate expectation computation

[Artzi and Zettlemoyer 2011; Zettlemoyer and Collins 2005]

Parsing

Learning

Modeling

- Structured perceptron
- A unified learning algorithm
- Supervised learning
- Weak supervision

## Modeling

Show me all papers about semantic parsing

↓ Parsing with CCG

$\lambda x. paper(x) \wedge topic(x, SEMPAR)$

What should these logical forms look like?

But why should we care?

# Modeling Considerations

Modeling is key to learning compact lexicons and high performing models

- Capture language complexity
- Satisfy system requirements
- Align with language units of meaning

Parsing

Learning

Modeling

- Semantic modeling for:
  - Querying databases
  - Referring to physical objects
  - Executing instructions

# Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the largest state?

# Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the largest state?

Noun Phrases

# Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the largest state?

Verbs

# Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the largest state?

Nouns

## Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital **of** Arizona?  
 How many states border California?  
 What is the largest state?

Prepositions

## Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the **largest** state?

Superlatives

## Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is **the** capital of Arizona?  
 How many states border California?  
 What is **the** largest state?

Determiners

## Querying Databases

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
AZ	Phoenix	2.7	CA	OR	Rainier	WA
			CA	NV	Shasta	CA

What is the capital of Arizona?  
 How many states border California?  
 What is the largest state?

Questions

## Referring to DB Entities

- Noun phrases Select single DB entities
- Prepositions Verbs Relations between entities
- Nouns Typing (i.e., column headers)
- Superlatives Ordering queries

## Noun Phrases

State		Mountains	
Abbr.	Capital	Name	State
AL	Montgomery	Bianca	CO
AK	Juneau	Antero	CO
AZ	Phoenix	Rainier	WA
WA	Olympia	Shasta	CA
NY	Albany		
IL	Springfield		

Noun phrases name specific entities

Washington  
WA

Florida  
FL

The Sunshine State  
FL

e-typed entities



## Noun Phrases

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

### Mountains

Name	State
Bianca	CO
Antero	CO
Rainier	WA
Shasta	CA

Noun phrases name specific entities

Washington

$\frac{NP}{WA}$

The Sunshine State

$\frac{NP}{FL}$

## Verb Relations

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

### Border

State1	State2
WA	OR
WA	ID
CA	OR
CA	NV

Verbs express relations between entities

Nevada **borders** California

$border(NV, CA)$

*true*

## Verb Relations

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

Nevada

$\frac{NP}{NV}$

borders

$\frac{S \setminus NP / NP}{\lambda x. \lambda y. border(y, x)}$

California

$\frac{NP}{CA}$

$S \setminus NP$

$\lambda y. border(y, CA)$

$S$

$border(NV, CA)$

## Nouns

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

### Mountains

Name	State
Bianca	CO
Antero	CO
Rainier	WA
Shasta	CA

Nouns are functions that define entity type

state

$\lambda x. state(x)$

{ WA, AL, AK, ... }

mountain

$\lambda x. mountain(x)$

{ BIANCA, ANTERO, ... }

$e \rightarrow t$   
functions  
define sets

## Nouns

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

### Mountains

Name	State
Bianca	CO
Antero	CO
Rainier	WA
Shasta	CA

Nouns are functions that define entity type

state

$\frac{N}{\lambda x. state(x)}$

mountain

$\frac{N}{\lambda x. mountain(x)}$

## Prepositions

### State

Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

### Mountains

Name	State
Bianca	CO
Antero	CO
Rainier	WA
Shasta	CA

Prepositional phrases are conjunctive modifiers

mountain in Colorado

$\lambda x. mountain(x) \wedge$

$in(x, CO)$

{ BIANCA, ANTERO }

## Prepositions

State				
Abbr.	Capital		in	Colorado
AL	Montgomery	$N$	$PP/NP$	$NP$
AK	Juneau	$\lambda x.mountain(x)$	$\lambda y.\lambda x.in(x, y)$	$CO$
AZ	Phoenix		$PP$	
WA	Olympia		$N \setminus N$	
NY	Albany		$\lambda f.\lambda x.f(x) \wedge in(x, CO)$	
IL	Springfield	$N$		
		$\lambda x.mountain(x) \wedge in(x, CO)$		

## Function Words

State		Border		
Abbr.	Capital	State1	State2	
AL	Montgomery	WA	OR	Certain words are used to modify syntactic roles state <b>that</b> borders California $\lambda x.state(x) \wedge border(x, CA)$ $\{OR, NV, AZ\}$
AK	Juneau	WA	ID	
AZ	Phoenix	CA	OR	
WA	Olympia	CA	NV	
NY	Albany			
IL	Springfield			

## Function Words

State				
Abbr.	Capital	state	that	borders
AL	Montgomery	$N$	$PP/(S \setminus NP)$	$S \setminus NP / NP$
AK	Juneau	$NV$	$\lambda f.f$	$\lambda x.\lambda y.border(y, x)$
AZ	Phoenix			$S \setminus NP$
WA	Olympia			$\lambda y.border(y, CA)$
NY	Albany			$PP$
IL	Springfield			$\lambda y.border(y, CA)$
				$N \setminus N$
				$\lambda f.\lambda y.f(y) \wedge border(y, CA)$
		$N$		
		$\lambda x.state(x) \wedge border(x, CA)$		

## Function Words

State		Border		
Abbr.	Capital	State1	State2	
AL	Montgomery	WA	OR	Certain words are used to modify syntactic roles <ul style="list-style-type: none"> <li>May have other senses with semantic meaning</li> <li>May carry content in other domains</li> </ul>
AK	Juneau	WA	ID	
AZ	Phoenix	CA	OR	
WA	Olympia	CA	NV	
NY	Albany			
IL	Springfield			

Other common function words: which, of, for, are, is, does, please

## Definite Determiners

State		Mountains		
Abbr.	Capital	Name	State	
AL	Montgomery	Bianca	CO	Definite determiner selects the single members of a set when such exists $\iota : (e \rightarrow t) \rightarrow e$
AK	Juneau	Antero	CO	
AZ	Phoenix	Rainier	WA	
WA	Olympia	Shasta	CA	
NY	Albany			
IL	Springfield			

the mountain in Washington  
 $\iota x.mountain(x) \wedge in(x, WA)$

$\{RAINIER\} \rightarrow RAINIER$

## Definite Determiners

State		Mountains		
Abbr.	Capital	Name	State	
AL	Montgomery	Bianca	CO	Definite determiner selects the single members of a set when such exists $\iota : (e \rightarrow t) \rightarrow e$
AK	Juneau	Antero	CO	
AZ	Phoenix	Rainier	WA	
WA	Olympia	Shasta	CA	
NY	Albany			
IL	Springfield			

the mountain in Colorado  
 $\iota x.mountain(x) \wedge in(x, CO)$

$\{BIANCA, ANTERO\} \rightarrow \text{X}$   
 No information to disambiguate

## Definite Determiners

State			
Abbr.	Capital		
AL	Montgomery	the $\frac{NP/N}{\lambda f. \lambda x. f(x)}$	mountain in Colorado
AK	Juneau		.
AZ	Phoenix		.
WA	Olympia		.
NY	Albany		.
IL	Springfield		.

$$\frac{\lambda x. mountain(x) \wedge in(x, CO)}{N}$$

$$\frac{NP}{\lambda x. mountain(x) \wedge in(x, CO)}$$

## Indefinite Determiners

State		Mountains		
Abbr.	Capital	Name	State	
AL	Montgomery	Bianca	CO	Indefinite determiners are select any entity from a set without a preference $\mathcal{A} : (e \rightarrow t) \rightarrow e$
AK	Juneau	Antero	CO	
AZ	Phoenix	Rainier	WA	
WA	Olympia	Shasta	CA	
NY	Albany			
IL	Springfield			

state with a mountain

$$\lambda x. state(x) \wedge in(\lambda y. mountain(y), x)$$

$$\lambda x. state(x) \wedge \exists y. mountain(y) \wedge in(y, x)$$

Exists

[Steedman 2011; Arzti and Zettlemoyer 2013b]

## Indefinite Determiners

state	with	a	mountain
$\frac{N}{\lambda x. state(x)}$	$\frac{PP/NP}{\lambda x. \lambda y. in(x, y)}$	$\frac{NP/N}{\lambda f. \lambda x. f(x)}$	$\frac{N}{\lambda x. mountain(x)}$
$\frac{NP}{\lambda x. mountain(x)}$			
$\frac{PP}{\lambda y. (\lambda x. mountain(x), y)}$			
$\frac{N \setminus N}{\lambda f. \lambda y. f(y) \wedge (\lambda x. mountain(x), y)}$			
$\frac{N}{\lambda y. state(y) \wedge (\lambda x. mountain(x), y)}$			

## Indefinite Determiners

a	
$\frac{PP \setminus (PP/NP)/N}{\lambda f. \lambda g. \lambda y. \exists x. g(x, y) \wedge f(x)}$	
a	
$\frac{S \setminus NP \setminus (S \setminus NP/NP)/N}{\lambda f. \lambda g. \lambda y. \exists x. g(x, y) \wedge f(x)}$	→
a	$\frac{NP/N}{\lambda f. \lambda x. f(x)}$
$\frac{S \setminus (S \setminus NP)/N}{\lambda f. \lambda g. \lambda y. \exists x. g(x, y) \wedge f(x)}$	

Using the indefinite quantifier simplifies CCG handling of the indefinite determiner

## Superlatives

State			
Abbr.	Capital	Pop.	
AL	Montgomery	3.9	Superlatives select optimal entities according to a measure the largest state $argmax(\lambda x. state(x), \lambda y. pop(y))$ Min or max ... over this set ... according to this measure
AK	Juneau	0.4	
AZ	Phoenix	2.7	
WA	Olympia	4.1	
NY	Albany	17.5	
IL	Springfield	11.4	

{ WA, AL, AK, ... }

AL	3.9
AK	0.4
Seattle	2.7
San Francisco	4.1
NY	17.5
IL	11.4

## Superlatives

State			
Abbr.	Capital	Pop.	
AL	Montgomery	3.9	Superlatives select optimal entities according to a measure the largest state $argmax(\lambda x. state(x), \lambda y. pop(y))$ Min or max ... over this set ... according to this measure
AK	Juneau	0.4	
AZ	Phoenix	2.7	
WA	Olympia	4.1	
NY	Albany	17.5	
IL	Springfield	11.4	

CA

AL	3.9
AK	0.4
Seattle	2.7
San Francisco	4.1
NY	17.5
IL	11.4

## Superlatives

State	
Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

the largest		state
$NP/N$		$N$
$\lambda f. \text{argmax}(\lambda x. f(x), \lambda y. \text{pop}(y))$		$\lambda x. \text{state}(x)$
$NP$		
$\text{argmax}(\lambda x. \text{state}(x), \lambda y. \text{pop}(y))$		

## Superlatives

State	
Abbr.	Capital
AL	Montgomery
AK	Juneau
AZ	Phoenix
WA	Olympia
NY	Albany
IL	Springfield

the most		populated	state
$NP/N/N$		$N$	$N$
$\lambda g. \lambda f. \text{argmax}(\lambda x. f(x), \lambda y. g(y))$		$\lambda x. \text{pop}(x)$	$\lambda x. \text{state}(x)$
$NP/N$			
$\lambda f. \text{argmax}(\lambda x. f(x), \lambda y. \text{pop}(y))$			
$NP$			
$\text{argmax}(\lambda x. \text{state}(x), \lambda y. \text{pop}(y))$			

## Representing Questions

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
			CA	OR	Rainier	WA

Which mountains are in Arizona?

```
SELECT Name FROM Mountains
WHERE State == AZ
```

Represent questions as the queries that generate their answers

Reflects the query SQL

## Representing Questions

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
			CA	OR	Rainier	WA

Which mountains are in Arizona?

$$\lambda x. \text{mountain}(x) \wedge \text{in}(x, AZ)$$

Represent questions as the queries that generate their answers

Reflects the query SQL

## Representing Questions

State			Border		Mountains	
Abbr.	Capital	Pop.	State1	State2	Name	State
AL	Montgomery	3.9	WA	OR	Bianca	CO
AK	Juneau	0.4	WA	ID	Antero	CO
			CA	OR	Rainier	WA

How many states border California?

$$\text{count}(\lambda x. \text{state}(x) \wedge \text{border}(x, CA))$$

Represent questions as the queries that generate their answers

Reflects the query SQL

## DB Queries

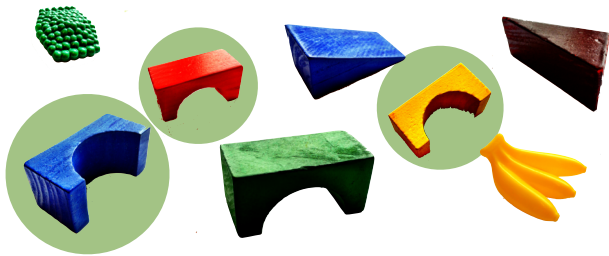
So Far

- Refer to entities in a database
- Query over type of entities, order and other database properties

Next

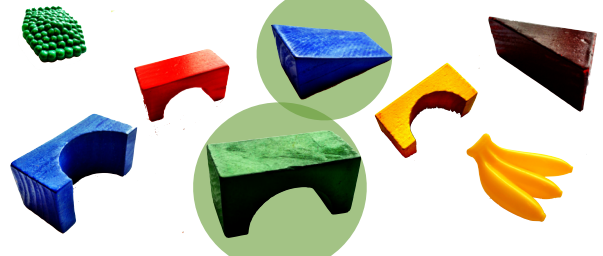
- How does this approach hold for physical objects?
- What do we need to change? Add?

## Referring to Real World Objects



all the arches except the green arch

## Referring to Real World Objects



the blue triangle and the green arch

## Plurality



arches

$\lambda x.arch(x)$



the arches

$\iota x.arch(x)$



## Plurality



blue blocks

$\lambda x.blue(x) \wedge block(x)$



brown block

$\lambda x.brown(x) \wedge block(x)$



## Plurality



- All entities are sets
- Space of entities includes singletons and sets of multiple objects

Cognitive evidence for sets being a primitive type

[Scontras et al. 2012]

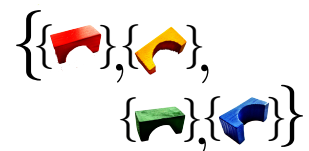
## Plurality



Plurality is a modifier and entities are defined to be sets.

arch

$\lambda x.arch(x) \wedge sg(x)$



## Plurality



Plurality is a modifier and entities are defined to be sets.

arches

$\lambda x.arch(x) \wedge plu(x)$

$\{\{red, yellow, blue, green\},$   
 $\{red, blue\}, \dots\}$

## Plurality and Determiners



Definite determiner must select a single set. E.g., heuristically select the maximal set.

the arches

$\iota x.arch(x) \wedge plu(x)$

$\{\{red, yellow, blue, green\}\}$

## Adjectives



Adjectives are conjunctive modifiers

blue objects

$\lambda x.blue(x) \wedge obj(x) \wedge plu(x)$

$\{\{blue, blue\}\}$

## DBs and Physical Objects

- Describe and refer to entities
- Ask about objects and relations between them
- Next: move into more dynamic scenarios

States		Borders	
Abbr.	Capital	State1	State2
AL	Montgomery	WA	OR
WA	Seattle	WA	ID
		CA	OR



## Beyond Queries

Noun phrases

Specific entities

Nouns

Sets of entities

Prepositional phrases  
Adjectives

Constrain sets

Questions

Queries to generate response

Works well for natural language interfaces for DBs

How can we use this approach for other domains?

## Procedural Representations

- Common approach to represent instructional language
- Natural for executing commands

go forward along the stone hall to the intersection with a bare concrete hall

*Verify(front : GRAVEL\_HALL)*

*Travel()*

*Verify(side : CONCRETE\_HALL)*

## Procedural Representations

- Common approach to represent instructional language
- Natural for executing commands

leave the room and go right

```
do_seq(verify(room(current_loc)),
      move_to(unique_thing( $\lambda x.$  equals(distance(x), 1))),
      move_to(right_loc))
```

[Matuszek et al. 2012b]

## Procedural Representations

- Common approach to represent instructional language
- Natural for executing commands

Click Start, point to Search, and the click For Files and Folders. In the Search for box, type "msdownld.tmp".

```
LEFT_CLICK(Start)
LEFT_CLICK(Search)
...
TYPE_INFO(Search for:, "msdownld.tmp")
```

[Branavan et al. 2009, Branavan et al. 2010]

## Procedural Representations

Dissonance between structure of semantics and language



- Poor generalization of learned models
- Difficult to capture complex language

## Spatial and Instructional Language

### Name objects

Noun phrases

Specific entities

Nouns

Sets of entities

Prepositional phrases  
Adjectives

Constrain sets

### Instructions to execute

Verbs

Davidsonian events

Imperatives

Sets of events

## Modeling Instructions

Describing an environment



Executing instructions

Agent



- Model actions and imperatives
- Consider how the state of the agent influences its understanding of language

## Modeling Instructions

place your back against the wall of the t intersection

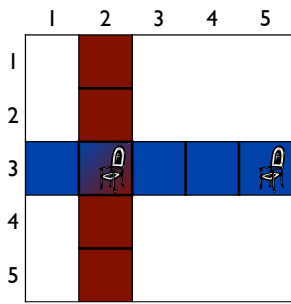
turn left

go forward along the pink flowered carpet hall two segments to the intersection with the brick hall

⋮

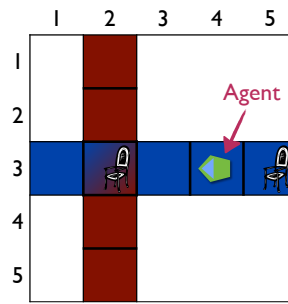


## Instructional Environment



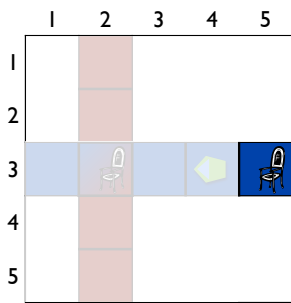
- Maps are graphs of connected positions
- Positions have properties and contain objects

## Instructional Environment



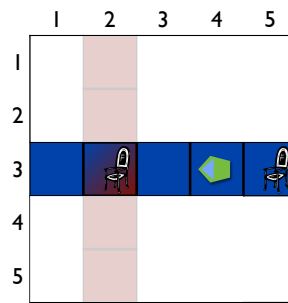
- Agent can move forward, turn right and turn left
- Agent perceives clusters of positions
- Clusters capture objects

## Instructional Environment



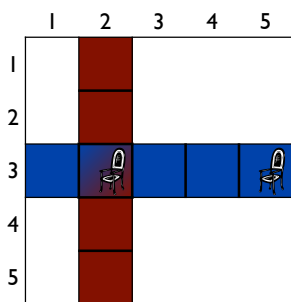
- Agent can move forward, turn right and turn left
- Agent perceives clusters of positions
- Clusters capture objects

## Instructional Environment



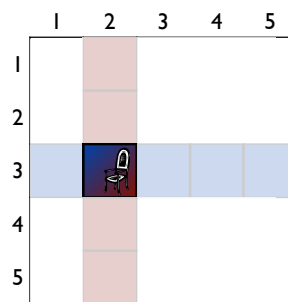
- Agent can move forward, turn right and turn left
- Agent perceives clusters of positions
- Clusters capture objects

## Instructional Environment



- Refer to objects similarly to our previous domains
- "Query" the world

## Grounded Resolution of Determiners



Nouns denote sets of objects

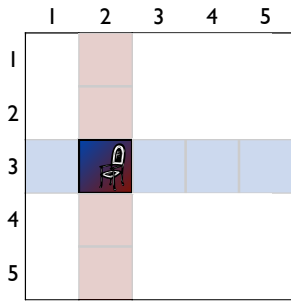
chair

$\lambda x.chair(x)$





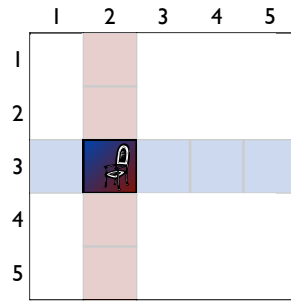
### Grounded Resolution of Determiners



Definite determiner selects a single entity

the chair  
 $\iota x.chair(x)$

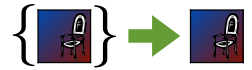
### Grounded Resolution of Determiners



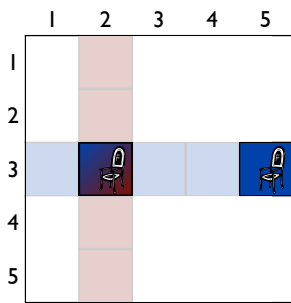
Definite determiner selects a single entity

the chair  
 $\iota x.chair(x)$

$$\iota : (e \rightarrow t) \rightarrow e$$



### Grounded Resolution of Determiners

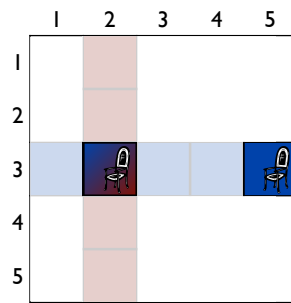


Definite determiner selects a single entity

the chair  
 $\iota x.chair(x)$

Fail?

### Grounded Resolution of Determiners

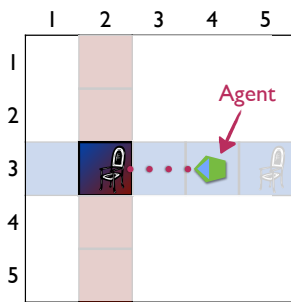


Definite determiner selects a single entity

the chair  
 $\iota x.chair(x)$

Must disambiguate to select a single entity

### Grounded Resolution of Determiners



Definite determiner selects a single entity

the chair  
 $\iota x.chair(x)$

Definite determiner depends on agent state



### Modeling Instructions

Events taking place in the world

Events refer to environment

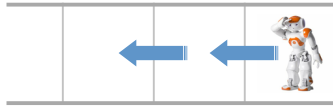
Implicit requests

## Modeling Instructions

Events taking place in the world

Events refer to environment

Implicit requests



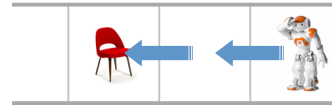
walk forward twice

## Modeling Instructions

Events taking place in the world

Events refer to environment

Implicit requests



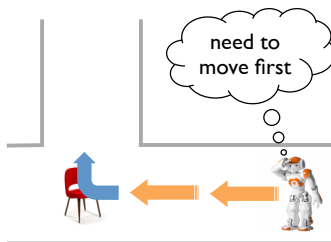
move twice to the chair

## Modeling Instructions

Events taking place in the world

Events refer to environment

Implicit requests



at the chair, turn right

## Davidsonian Event Semantics

- Actions in the world are constrained by adverbial modifiers
- The number of such modifiers is flexible

Adverbial modification is thus seen to be logically on a par with adjectival modification: what adverbial clauses modify is not verbs, but the events that certain verbs introduce.

Davidson 1969 (quoted in Maienborn et al. 2010)

[Davidson 1967]

## Davidsonian Event Semantics

- Use event variable to represent events
- Verbs describe events like nouns describe entities
- Adverbials are conjunctive modifiers

Vincent shot Marvin in the car accidentally

$$\exists a.shot(a, VINCENT, MARVIN) \wedge in(a, ix.car(x)) \wedge \neg intentional(a)$$

[Davidson 1967]

## Neo-Davidsonian Event Semantics

Active

Vincent shot Marvin

$$\exists a.shot(a, VINCENT, MARVIN)$$

Passive

Marvin was shot (by Vincent)

Agent optional in passive

[Parsons 1990]

## Neo-Davidsonian Event Semantics

**Active** Vincent shot Marvin  
 $\exists a.shot(a, VINCENT, MARVIN)$

**Passive** Marvin was shot (by Vincent)  
 $\exists a.shot(a, MARVIN)$

Agent optional in passive

Can we represent such distinctions without requiring different arity predicates?

[Parsons 1990]

## Neo-Davidsonian Event Semantics

- Separation between semantic and syntactic roles
- Thematic roles captured by conjunctive predicates

Vincent shot Marvin  
 $\exists a.shot(a, VINCENT, MARVIN)$



$\exists a.shot(a) \wedge agent(a, VINCENT) \wedge patient(a, MARVIN)$

[Parsons 1990]

## Neo-Davidsonian Event Semantics

Vincent shot Marvin in the car accidentally

$\exists a.shot(a) \wedge agent(a, VINCENT) \wedge patient(a, MARVIN) \wedge in(a, ix.car(x)) \wedge \neg intentional(a)$

- Decomposition to conjunctive modifiers makes incremental interpretation simpler
- Shallow semantic structures: no need to modify deeply embedded variables

[Parsons 1990]

## Neo-Davidsonian Event Semantics

$\exists a.shot(a) \wedge agent(a, VINCENT) \wedge patient(a, MARVIN) \wedge in(a, ix.car(x)) \wedge \neg intentional(a)$

Without events:

$shot(VINCENT, MARVIN, ix.car(x), INTENTIONAL)$

- Decomposition to conjunctive modifiers makes incremental interpretation simpler
- Shallow semantic structures: no need to modify deeply embedded variables

[Parsons 1990]

## Representing Imperatives



- Imperatives define actions to be executed
- Constrained by adverbials
- Similar to how nouns are defined

## Representing Imperatives



- Imperatives are sets of actions
- Just like nouns: functions from events to truth

$f : ev \rightarrow t$

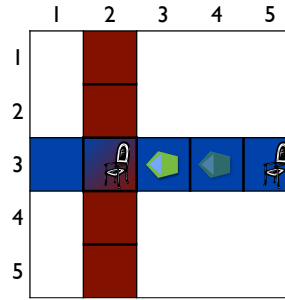
## Representing Imperatives



Given a set, what do we actually execute?

- Need to select a single action and execute it
- Reasonable solution: select simplest/shortest

## Modeling Instructions



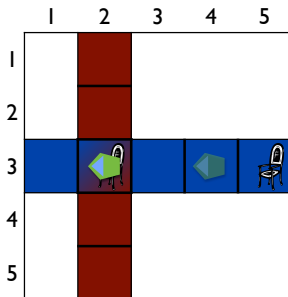
- Imperatives are sets of events
- Events are sequences of identical actions

move  
 $\lambda a.move(a)$



Disambiguate by preferring shorter sequences

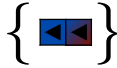
## Modeling Instructions



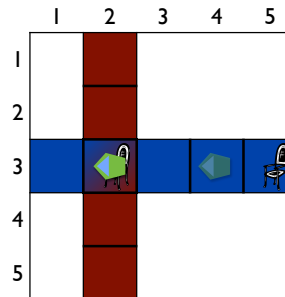
Events can be modified by adverbials

move twice

$\lambda a.move(a) \wedge len(a, 2)$



## Modeling Instructions



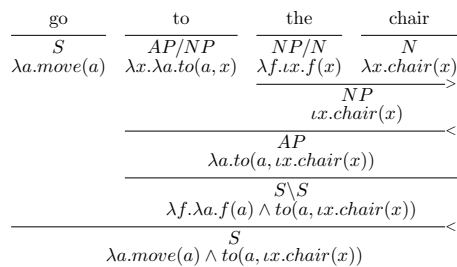
Events can be modified by adverbials

go to the chair

$\lambda a.move(a) \wedge to(a, ix.chair(x))$

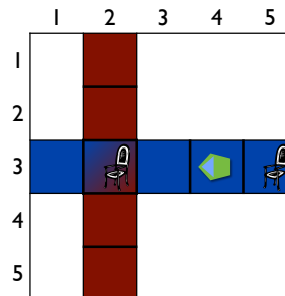


## Modeling Instructions



Treatment of events and their adverbials is similar to nouns and prepositional phrases

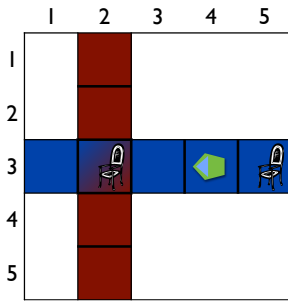
## Modeling Instructions



Dynamic Models

Implicit Actions

## Dynamic Models



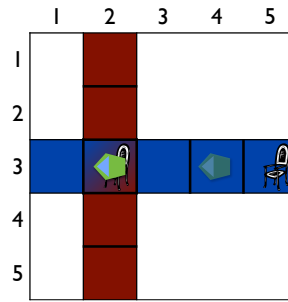
World model changes during execution

move until you reach the chair

$\lambda a.move(a) \wedge$   
 $post(a, intersect(\lambda x.chair(x), you))$



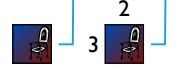
## Dynamic Models



World model changes during execution

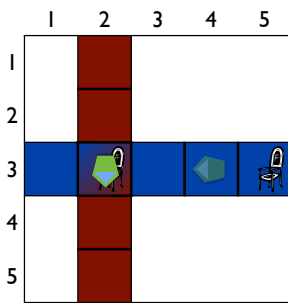
move until you reach the chair

$\lambda a.move(a) \wedge$   
 $post(a, intersect(\lambda x.chair(x), you))$   
 Update



Update model to reflect state change

## Implicit Actions



Consider action assignments with prefixed implicit actions

at the chair, turn left

$\lambda a.turn(a) \wedge dir(a, left) \wedge$   
 $pre(a, intersect(\lambda x.chair(x), you))$



## Experiments

Instruction:

at the chair, move forward three steps past the sofa

Demonstration:

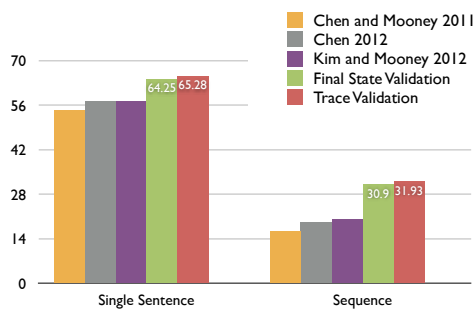


- Situated learning with joint inference
- Two forms of validation
- Template-based  $GENLEX(x, \mathcal{V}; \Lambda, \theta)$

[Artzi and Zettlemoyer 2013b]

## Results

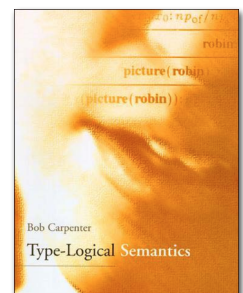
### SAIL Corpus - Cross Validation



[Artzi and Zettlemoyer 2013b]

## More Reading about Modeling

Type-Logical Semantics  
 by Bob Carpenter



[Carpenter 1997]

# Today

Parsing Combinatory Categorical Grammars

Learning Unified learning algorithm

Modeling Best practices for semantics design

# Looking Forward

## Looking Forward: Scale

**Goal** Answer any question posed to large, community authored databases

**Challenges**

- Large domains
- Scalable algorithms
- Unseen words and concepts

**See** Cai and Yates 2013a, 2013b



What are the neighborhoods in New York City?  
 $\lambda x. \text{neighborhoods}(\text{new\_york}, x)$

How many countries use the rupee?  
 $\text{count}(x). \text{countries.used}(\text{rupee}, x)$

How many Peabody Award winners are there?  
 $\text{count}(x). \exists y. \text{award\_honor}(y) \wedge \text{award\_winner}(y, x) \wedge \text{award}(y, \text{peabody\_award})$

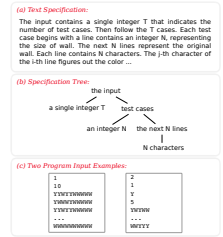
## Looking Forward: Code

**Goal** Program using natural language

**Challenges**

- Data
- Complex intent
- Complex output

**See** Kushman and Barzilay 2013; Lei et al. 2013



Text Description	Regular Expression
three letter word starting with 'X'	$\text{X}[A-Z]{2}$

## Looking Forward: Context

**Goal** Understanding how sentence meaning varies with context

**Challenges**

- Data
- Linguistics: co-ref, ellipsis, etc.

**See** Miller et al. 1996; Zettlemoyer and Collins 2009; Artzi and Zettlemoyer 2013

Example #1:  
 (a) show me the flights from boston to philly  
 $\lambda x. \text{flight}(x) \wedge \text{from}(x, \text{bos}) \wedge \text{to}(x, \text{phi})$   
 (b) show me the ones that leave in the morning  
 $\lambda x. \text{flight}(x) \wedge \text{from}(x, \text{bos}) \wedge \text{to}(x, \text{phi}) \wedge \text{during}(x, \text{morning})$   
 (c) what kind of plane is used on these flights  
 $\lambda y. \exists x. \text{flight}(x) \wedge \text{from}(x, \text{bos}) \wedge \text{to}(x, \text{phi}) \wedge \text{during}(x, \text{morning}) \wedge \text{aircraft}(x) = y$

Example #2:  
 (a) show me flights from milwaukee to orlando  
 $\lambda x. \text{flight}(x) \wedge \text{from}(x, \text{mil}) \wedge \text{to}(x, \text{orl})$   
 (b) cheapest  
 $\text{argmin}(\lambda x. \text{flight}(x) \wedge \text{from}(x, \text{mil}) \wedge \text{to}(x, \text{orl}), \lambda y. \text{fare}(y))$   
 (c) departing wednesday after 5 o'clock  
 $\text{argmin}(\lambda x. \text{flight}(x) \wedge \text{from}(x, \text{mil}) \wedge \text{to}(x, \text{orl}) \wedge \text{day}(x, \text{wed}) \wedge \text{depart}(x) > 1700, \lambda y. \text{fare}(y))$

## Looking Forward: Sensors

**Goal** Integrate semantic parsing with rich sensing on real robots

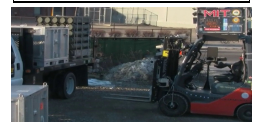
**Challenges**

- Data
- Managing uncertainty
- Interactive learning

**See** Matuszek et al. 2012; Tellex et al. 2013; Krishnamurthy and Kollar 2013



Move the pallet from the truck.  
 Remove the pallet from the back of the truck.  
 Offload the metal crate from the truck.



# UW SPF

Open source semantic parsing framework

<http://yoavartzi.com/spf>

Semantic  
Parser

Flexible High-Order  
Logic Representation

Learning  
Algorithms

Includes ready-to-run examples

[Artzi and Zettlemoyer 2013a]

[fin]

## Supplementary Material

### Function Composition

$$g_{\langle\alpha,\beta\rangle} = \lambda x.G$$

$$f_{\langle\beta,\gamma\rangle} = \lambda y.F$$

$$g(A) = (\lambda x.G)(A) = G[x := A]$$

$$f(g(A)) = (\lambda y.F)(G[x := A]) = F[y := G[x := A]]$$

$$\lambda x.f(g(A))[A := x] =$$

$$\lambda x.F[y := G[x := A]][A := x] =$$

$$\lambda x.F[y := G] = (f \cdot g)_{\langle\alpha,\gamma\rangle}$$